suRv’s up: Statistical software for the surveillance of infectious diseases

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Outline

1. The surveillance package
   - Introduction

2. Discrete time and discrete space data

3. Continuous time discrete space data
   - 1861 Hagelloch measles epidemic
   - The twinSIR model class

4. Continuous time continuous space epidemic data
   - The twinstim model class
   - Invasive meningococcal disease surveillance data

5. Discussion

Sections 3 and 4 contain large programming contributions from Sebastian Meyer, München, Germany
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Infectious disease modelling and monitoring in practice (1)

- Early detection of a rapid increase in the incidence of a notifiable infectious disease depends on a good surveillance system and skilled epidemiologists to analyse the data.
- Statistical software helps the good epidemiologist become even better:
  - Models and their associated inference can be used to gain insights into disease dynamics.
  - Large data streams can be monitored simultaneously to quickly detect incidence changes.
  - Reports of these investigations can be generated automatically.
- There appears to be a lack of general purpose software for routine infectious disease modelling and monitoring.
Infectious disease modelling and monitoring in practice (2)

Good software alone does not do the job. It also takes:

- An understanding of the statistical aspects of the models and their selection
- A fair compromise between resources available and cost for acquisition, installation and training.
- Didactic documentation of the software containing illustrations of its use on relevant datasets
- A convincing answer to the question: *what’s the added value?*

**Aim of this talk**

Introduce an open source R package for the visualization, modelling and monitoring of routinely collected public health surveillance data
The R package surveillance (1)

- Prospective monitoring for univariate count data time series:
  - farrington – Farrington et al. (1996)
  - cusum – Rossi et al. (1999) and extensions
  - bayes – H. (2007)\(^1\)
  - outbreakP – Frisén et al. (2009)

- Prospective changepoint detection for categorical time series:
  - pairedbinCUSUM – surgical performance (Steiner et al., 2000)

\(^1\)For a Bayesian GAM extension: Talk A1 by J. Manitz (Wed 11:15-11:45).
The R package surveillance (2)

- Retrospective count data time series models:
  - **hhh** – Held et al. (2005); Paul et al. (2008)
  - **hhh4** – Paul and Held (2011)
  - **twins** – Held et al. (2006)

- Spatio-Temporal point process modelling and monitoring:
  - **twinstim** – Meyer et al. (2010)
  - **stcd** – continuous space - continuous time cluster detection (Assunção and Correa, 2009)

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3 See poster 'Spatio-temporal modelling of infectious disease surveillance data using the R-package surveillance' by M. Paul.
The R package surveillance (3)

- **Motivation**: Provide data structure and implementation framework for methodological developments in surveillance
- **Spin-off**: Tool for epidemiologists and others working in applied infectious disease modelling and monitoring
- **Availability**: CRAN, current development version from http://surveillance.r-forge.r-project.org/
  under the GNU General Public License (GPL) v. 2.0.
- To install the development version 1.3.0 under R version 2.12:

```r
> install.packages("surveillance", repos = "http://r-forge.r-project.org")
> library("surveillance")
```
Use of surveillance in practice

A number of public health institutions and projects use the package, especially for outbreak detection:

- Computer Assisted Search For Epidemics (CASE) project by the Swedish Institute for Infectious Disease Control (SMI) – Cakici et al. (2010)
- Project on understanding Disease Risks from Livestock Movement in the Greater Mekong Subregion (Anonymous, 2011)
- Governmental Institute of Public Health, Lower Saxony, Germany (Hulth et al., 2010)
- Finish National Institute for Health and Welfare
This talk will...

- Focus on statistical modelling, because modelling provides insight into the spatio-temporal disease dynamics and thus is a precondition for monitoring.
- Differentiate methods based on the spatial and temporal resolution of the available data → trend towards more accurate temporal and geocoded information
- Give a software oriented view with less focus on mathematical detail.
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Surveillance data as multivariate time series of counts (1)

- Data from surveillance systems is, after suitable preprocessing, available as multivariate time series of counts
  \[ \{y_{it}; i = 1, \ldots, m, t = 1, \ldots, n\}. \]
- The surveillance class for such data is the `sts` class.

```r
> data("measlesDE")
> measlesDE

-- An object of class sts --
  freq: 52
  start: 2005 1
  dim(observations): 156 16

  Head of observations:
  Baden-Wuerttemberg Bavaria Berlin Brandenburg Bremen Hamburg Hesse
  [1,] 0 0 0 0 0 1 3
  Mecklenburg-Western Pomerania Lower Saxony North Rhine-Westphalia
  [1,] 0 0 0 0
  Rhineland-Palatinate Saarland Saxony Saxony-Anhalt Schleswig-Holstein
  [1,] 0 0 1 0 0
  Thuringia
  [1,] 0
  ...
```
Surveillance data as multivariate time series of counts (2)

> `plot(measlesDE, type = observed ~ time | unit)`
Outbreak detection using Farrington’s algorithm (1)

- The Farrington et al. (1996) algorithm is an early statistical algorithm to quickly detect emerging outbreaks in univariate count data time series based on an overdispersed Poisson GLM with intercept and trend:

\[
E(y_t) = \mu_t = \exp(\beta_0 + \beta_1 \cdot t),
\]

\[
\text{Var}(y_t) = \phi \cdot \mu_t.
\]

- For each time point, the GLM is fitted and a \((1 - \alpha) \cdot 100\%\) prediction interval is computed.
- If the current observation is larger than the upper limit of the prediction interval, then an alarm is generated.
Outbreak detection using Farrington’s algorithm (2)

The implementation in surveillance:

```r
> twostates <- measlesDE[, c("Bavaria", "North Rhine-Westphalia")]
> s <- farrington(twostates, control = list(range = 110:nrow(twostates), + b = 2, w = 5))
```
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Hagelloch measles epidemic

- Measles outbreak among 188 children (age $\leq 14$) during the winter 1861 in the German city of Hagelloch (near Tübingen).
- Detailed data including school class, household and household location of cases is available (Pfeilsticker, 1863; Oesterle, 1992).
- Data is prototypical for single outbreak data, but routine monitoring aspects are present.

```r
> data("hagelloch")
> summary(hagelloch)

AN SIR EPIDEMIC
Time range: 0 -- 91.8102561747641
Number of individuals: 188
1 initially infected individuals:
"184"
0 never infected individuals
Size of the epidemic: 187
```

Hagelloch measles epidemic – epidemic curve

> library("epitools")
> hagelloch.df <- as.data.frame(hagelloch[hagelloch$BLOCK ==
+       1, ])
> with(hagelloch.df, epicurve.dates(PRO, strata = CL))
Hagelloch measles epidemic – SIR states

Visualization of epidemic as transition between states of a Susceptible-Infectious-Recovered (SIR) model:

```r
> plot(hagelloch)
```
Hagelloch measles epidemic – household locations

> coordinates(hagelloch.df) <- c("x.loc", "y.loc")
> plot(hagelloch.df, cex = sqrt(multiplicity.sp(hagelloch.df)))
The twinSIR Model (1)

- Continuous time stochastic process with conditional intensity functions parametrized by covariates
- Set of possible event locations is known beforehand
- Risk of infection consists of two components
  - **endemic component**: Time to infection from external sources modelled by a Cox model
  - **epidemic component**: Similar to heterogeneous SIR model with, e.g., distance weighting of infectives
- The two component modelling is inspired by a model for univariate disease count data time series (Held et al., 2006).
The twinSIR Model (2)

Conditional intensity function $\lambda_i(t|\mathcal{H}_t)$ for a state change from susceptible to infectious of individual $i$:

$$\lambda_i(t|\mathcal{H}_t) = Y_i(t) \cdot [h_i(t) + e_i(t|\mathcal{H}_t)],$$

$$h_i(t) = \exp \left( h_0(t) + z_i(t)'\beta \right),$$

$$e_i(t|\mathcal{H}_t) = \sum_{j \in I(t)} f_{ij} = \sum_{m=1}^{q} \alpha_m x_{im}(t) = x_i(t)'\alpha, \quad \alpha \geq 0$$

Notation: $\mathcal{H}_t$ is the history of the process, $Y_i(t)$ the at risk indicator, $h_0(t)$ the baseline hazard, $z_i(t)$ a time depending endemic covariate vector, $I(t)$ the set of infectious at $t$ and $f_{ij} \geq 0$ is a function of the covariates of $i$ and $j$, e.g., the Euclidean distance between $i$ and $j$ described by a spline-basis.
The twinSIR Model (3)

- H. (2009) describes penalized likelihood inference and model selection using one-sided AIC when $h_0(t)$ is given as a penalized spline.
- The function `twinSIR` provides a model formula oriented implementation for model fitting and residual analysis.
- We will analyse the Hagelloch data using class room and household indicators as in Neal and Roberts (2004), but with an additional endemic component handling several outbreaks:

$$\lambda_i(t|\mathcal{H}_t) = Y_i(t) \cdot \left[ \exp(\beta_0) + \alpha_{Hx_i,H}(t) + \alpha_{c1x_i,c1}(t) + \alpha_{c2x_i,c2}(t) + \alpha_{localx_i,local}(t) \right],$$

where $x_i,\cdot$ is an indicator of how many infectious are, e.g., in the same sample household as $i$. 
Analysing the Hagelloch data (2)

Result with surveillance:

```r
> m <- twinSIR(~c1 + c2 + household + local, data = hagelloch)
> summary(m)

Call:
twinSIR(formula = ~c1 + c2 + household + local, data = hagelloch)

Coefficients:
            Estimate Std. Error z value Pr(>|z|)  
c1           0.035261   0.007494  4.705  2.53e-06 ***  
c2           0.004127   0.000892  4.628  3.70e-06 ***  
household    0.030036   0.006281  4.782  1.74e-06 ***  
local        0.003682   0.000719  5.120  3.06e-07 ***  
cox(logbaseline) -6.215546  0.434573 -14.303  < 2e-16 ***
---
Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1

Total number of infections: 187

One-sided AIC: 1286.2  (simulated penalty weights)
Log-likelihood: -640.1
Number of log-likelihood evaluations: 68
```
Analysing the Hagelloch data (3)

Behaviour of the loglikelihood near the MLE:

```r
> prof <- profile(m, list(c(match("c1", names(coef(m))), NA, NA, 25),
+ c(match("c2", names(coef(m))), NA, NA, 25)))
```

![Graph showing the behaviour of the loglikelihood near the MLE with profile, estimated, and wald lines.](image-url)
Analysing the Hagelloch data (3)

> plot(m, what = "total intensity")
> plot(m, what = "epidemic proportion")
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Example: Invasive meningococcal disease (IMD)

- IMD is a life-threatening infectious disease triggered by the bacterium *Neisseria meningitidis* (aka *meningococcus*)
- Two most common finetypes in Germany in 2002–2008: 336 cases of *B:P1.7-2,4:F1-5*, 300 cases of *C:P1.5,2:F3-3*
- Case variables: date, coordinates of residence postcode, age, gender
- Scientific question: Do the finetypes spread differently?
- Statistical task: Quantify the transmission dynamics using two-component modelling of the conditional intensity function
Additive-multiplicative continuous space-time intensity model

\[ \lambda^*(t, s) = h(t, s) + e^*(t, s) \]
Additive-multiplicative continuous space-time intensity model

\[ \lambda^*(t, s) = h(t, s) + e^*(t, s) \]

- Multiplicative endemic component

\[ h(t, s) = \exp \left( o_{\xi(s)} + \beta' z_{\tau(t), \xi(s)} \right) \]

- Piecewise constant function on a spatio-temporal grid \( \{C_1, \ldots, C_D\} \times \{A_1, \ldots, A_M\} \) with time interval index \( \tau(t) \), region index \( \xi(s) \)

- Region-specific offset \( o_{\xi(s)} \), e.g. the log-population density

- Endemic linear predictor \( \beta' z_{\tau(t), \xi(s)} \) includes discretised time trend and exogenous effects, e.g. influenza cases
Additive-multiplicative continuous space-time intensity model

\[ \lambda^*(t, s) = h(t, s) + e^*(t, s) \]

Additive epidemic (self-exciting) component

\[ e^*(t, s) = \sum_{j \in I^*(t, s; \varepsilon, \delta)} e^{\eta_j} g_\alpha(t - t_j) f_\sigma(s - s_j) \]

- Individual infectivity weighting through linear predictor \( \eta_j = \gamma' m_j \) based on the vector of unpredictable marks
- Positive parametric interaction functions, e.g. \( f_\sigma(s) = \exp \left( -\frac{||s||^2}{2\sigma^2} \right) \) and \( g_\alpha(t) = e^{-\alpha t} \)
- Set of active infectives depends on fixed maximum temporal and spatial interaction ranges \( \varepsilon \) and \( \delta \)
Marked extension with event type

- Motivation: joint modelling of both finetypes of IMD
- Additional dimension $\mathcal{K} = \{1, \ldots, K\}$ for event type $\kappa \in \mathcal{K}$

Marked CIF

$$\lambda^*(t, s, \kappa) = \exp \left( \beta_{0,\kappa} + o\xi(s) + \beta' z(t), \xi(s) \right) + \sum_{j \in I^*(t,s;\varepsilon,\delta)} q_{\kappa_j,\kappa} e^{\eta_j} g(\alpha(t - t_j | \kappa_j) f(\sigma(s - s_j | \kappa_j))$$

- Type-specific endemic intercept
- Type-specific transmission, $q_{k,l} \in \{0, 1\}, k, l \in \mathcal{K}$
- Type-specific effect modification $\eta_j = \gamma' m_j$, $\kappa_j$ is part of $m_j$
- Type-specific interaction functions, e.g. variances $\sigma^2_{\kappa}$
An important quantity in epidemic modelling is the mean number of offspring each case generates. Since offspring are generated in time according to an inhomogeneous Poisson process we define

$$\mu_i = e^{\eta_i} \cdot \left[ \int_0^\infty g_\alpha(t) \, dt \right] \cdot \left[ \int_{b(0,\delta)} f_\sigma(s) \, ds \right], \quad i = 1, \ldots, N.$$  

Type specific reproduction numbers are obtained by averaging the $\mu_i$'s for each type.
The epidataCS S3 class

**events** SpatialPointsDataFrame object containing information about the space-time location of the individual cases and their covariates.

**W** SpatialPolygons object describing the observational region.

**stgrid** Spatial partitioning, $A$, of $W$ and a temporal partitioning, $C$, of $[0, T]$ together forming a space-time partition with $|A| \times |C|$ cells containing the endemic covariates as a data.frame.

**qmatrix** $\mathcal{K} \times \mathcal{K}$ indicator matrix defining possible interaction between different types.
Visualization of IMD data (1)

```r
> data("imdepi")
> class(imdepi)

[1] "epidataCS" "list"

> imdepi

History of an epidemic
Observation period: 0 -- 2562
Observation window (bounding box): [4034, 4670] x [2687, 3543]
Spatio-temporal grid (not shown): 366 time blocks, 413 tiles
Types of events: 'B' 'C'
Overall number of events: 636

coordinates ID  time  tile  type  eps.t  eps.s  sex  agegrp  BLOCK  start  popdensity
103 (4112.19, 3202.79)  1  0.21  05554  B  30  200  male  [3,19)  1  0  261
402 (4122.51, 3076.97)  2  0.71  05382  C  30  200  male  [3,19)  1  0  519
...
Visualization of IMD data (1)

```r
> with(imdepi, { plot(W) ; plot(events,add=TRUE) })
```

Finetype

- B
- C
Visualization of IMD data (3)

Spatio-temporal visualization of disease occurrence using the animation package Xie (2010). Produces animated GIF files or Flash animations:

```r
> animate(imdepi)
```
Analysis of IMD data (1)

```r
> m <- twinstim(endemic = ~1 + offset(log(popdensity)) + I(start/365) +
+     sin(start * 2 * pi/365) + cos(start * 2 * pi/365),
+     epidemic = ~1 + agegrp + type,
+     siaf = siaf_log1, data = imdepi, subset = allEpiCovNonNA,
+     optim.args = optim.args, finetune=FALSE,
+     nCub = 36,
+     typeSpecificEndemicIntercept = FALSE)

> toLatex(summary(m))
```

|                      | Estimate | Std. Error | z value | \( P(|Z| > |z|) \)  |
|----------------------|----------|------------|---------|---------------------|
| h.(Intercept)        | -20.3815 | 0.0874     | -233.25 | < 2 \cdot 10^{-16} |
| h.I(start/365)       | -0.0442  | 0.0223     | -1.98   | 0.047               |
| h.sin(start*2*pi/365) | 0.2643   | 0.0648     | 4.08    | 4.5 \cdot 10^{-05} |
| h.cos(start*2*pi/365) | 0.2627   | 0.0642     | 4.09    | 4.3 \cdot 10^{-05} |
| e.(Intercept)        | -12.5277 | 0.3236     | -38.71  | < 2 \cdot 10^{-16} |
| e.agegrp[3,19]       | 0.7054   | 0.3266     | 2.16    | 0.03078             |
| e.agegrp[19,Inf]     | -0.2076  | 0.4577     | -0.45   | 0.65013             |
| e.typeC              | -0.8900  | 0.2658     | -3.35   | 0.00081             |
| e.siaf.1             | 2.7708   | 0.0817     | 33.93   | < 2 \cdot 10^{-16} |

AIC: 18837
Log-likelihood: -9409
Analysis of IMD data (2)

$R_0$ calculations:

```r
> R0events <- RO(m, newevents = marks(imdepi))
> (R0.hat <- tapply(R0events, marks(imdepi)$type, mean,
+     na.rm = TRUE))

   B    C
0.24150 0.10171
```

To obtain CIs, simulate coefficients from asymptotic normal:

```r
> boot <- replicate(999, {
+   m$coefficients <- mvrnorm(1, mu = coef(m), Sigma = vcov(m))
+   R0events <- RO(m, newevents = marks(imdepi))
+   tapply(R0events, marks(imdepi)$type, mean, na.rm = TRUE)
+ })

> t(apply(cbind(R0.hat, boot), 1, quantile, p = c(0.025,
+   0.975)))

       2.5%    97.5%
B 0.185715 0.32314
C 0.065356 0.16601
```
Analysis of IMD data (3)

Visualization of the fitted spatial interaction function:

```r
> plotiaf(m, iaf = "siaf", cols = "black")
```

![Graph showing the fitted spatial interaction function with point estimates and 95% Wald confidence intervals.](image)
Analysis of IMD data (5)

Residual plot as in Ogata (1988) by considering Cox-Snell-like residuals based on the fitted cumulative intensity function:

```R
ger residuals(m, plot = TRUE)
```

![Cumulative distribution plot with 95% KS error bounds](image)
Simulation from a fitted twinstim model using an adaptation of Ogata’s modified thinning algorithm for marked point processes:

```r
> stpp <- simulate(m, nsim = 1,
+                   data = imdepi, tiles = kreise,
+                   t0 = 200, T = 300,
+                   W = W, nCub = 24)
>
> summary(stpp)$typeTable
   B  C
14 14

> with(stpp, {
+     plot(kreise)
+     plot(W, add = TRUE)
+     plot(events, add = TRUE)
+ })
```

Map showing the distribution of events with two types, B and C.
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Discussion (1)

- Talk presented steps towards R functionality for general modelling and monitoring of routine collected infectious disease data.
- `twinSIR` and `twinstim` provide data structures and inference framework for small- to medium-sized georeferenced event data (beyond epidemics!)
- Combining database, R, Sweave/odfWeave and LaTeX/OpenOffice allows for easy generation of reports
- R similarly can analyse outbreak investigation studies using logistic, conditional logistic and exact logistic regression.
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Literature III


URL http://CRAN.R-project.org/package=animation